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https://www-ljk.imag.fr/membres/Pierre.Karpman/tea.html

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Introduction 2021-02-03 1/29

# First things first

#### Main goals of this course:

- Motivate the field (why is cryptography useful?)
- Introduce some constructions (what's a block cipher, a key exchange?...)
- Introduce some attacks (how do you find collisions for a random function?...)
- ▶ Introduce some real-life usage (e.g. TLS)

Introduction 2021–02–03 2/29

### Schedule

#### Previous slide in order:

- Definitions and basic security notions for:
  - ▶ Block ciphers, symmetric encryption, MACs, hash functions
  - Discrete log-based key exchange & signatures, RSA (incl. paddings)
- A few examples of generic attacks
- A few concrete use-cases/applications/attacks

Introduction 2021-02-03 3/29

# Organisation

#### There will be:

- Lectures (such as this one)
- Tutorial sessions (mostly)
- Practical/lab sessions (occasionally)
- A contrôle continu evaluation (a small programming project)
- A final exam

Introduction 2021-02-03 4/29

### What's crypto?

Quick answer: it's about protecting secret data from adversaries

- ► In a communication (encrypted email, text messages; on the web; when paying by credit card)
- On a device (encrypted hard-drive)
- During a computation (online voting)
- ► Etc.

Introduction 2021-02-03 5/29

### Where does crypto run?

#### Crypto needs on various platforms

- ► High-end CPUs (Server/Desktop/Laptop computers,...)
- Mobile processors (Phones,...)
- Microcontrollers (Smartcards,...)
- Dedicated hardware (accelerating coprocessors, cheap chips,...)

Introduction 2021-02-03 **6/29** 

#### Techno constraints

#### Varying contexts, varying requirements

- Speed (throughput)
- Speed (latency)
- Code/circuit size
- Energy/power consumption
- Protection v. physical attacks
- ⇒ Implementation plays a big part in crypto

Introduction 2021–02–03 **7/29** 

### Quick example

### A protocol (e.g. TLS) uses among others

- A key exchange algorithm (e.g. Diffie-Hellman)
  - "public-key" cryptography
    - instantiated with a secure group (e.g. ANSSI FRP256V1)
- ► An authenticated-encryption mode of operation (e.g. GCM)
  - "symmetric-key" cryptography
    - instantiated with a secure block cipher (e.g. the AES)
- A digital signature algorithm (e.g. ECDSA)
  - "public-key" + "symmetric-key" cryptography
    - instantiated with a secure group and a secure hash function (e.g. SHA-3)

Introduction 2021-02-03 8/29

### Protocols can be complex

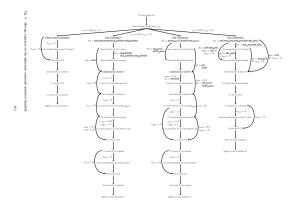


Figure: Part of the TLS state machine, Beurdouche et al., 2015

Introduction 2021-02-03 9/29

### "Doing crypto"

- Designing new primitives/constructions(/protocols)
- Analysing existing primitives/...
- Deploying crypto in products
- Different goals, different techniques
  - Ad-hoc analysis, discrete mathematics, algorithmics
  - Computational number theory/algebraic geometry
  - Low-level implementation (assembly, hardware)
  - Formal methods
  - Following "good practice"

Introduction 2021–02–03 10/29

### Scope of an analysis

#### Many types of adversary

- Passive ("eavesdropper = Eve")
- ▶ Not passive, i.e. active
- With or w/o physical access
  - Side channels
  - Fault attacks
- With varying scenarios ("one-time" or long-term secret?)
- With varying objectives

Introduction 2021–02–03 11/29

# Security objectives?

Introduction 2021–02–03 12/29

### Security objectives?

- ► Hard to find the "keys"
- Hard to find the message (confidentiality)
- Hard to change/forge a message (integrity/authenticity)
- Etc.

#### Remark

Most of the time, one aims for some form of *computational* security: it is always possible to break everything by spending "enough" time → just make sure that "enough" is "too much".

Introduction 2021–02–03 12/29

### A broader perspective

In crypto (as in science in general), we need:



Figure: Nebular's wisdom (Watterson)

Introduction 2021-02-03 13/29

### Definitions for science!

#### It is essential to properly define:

- The objects we use, e.g. what kind of basic functionality ("API") is required (so that there's no ambiguity about what we're talking about)
- ► The properties we want the objects to further satisfy, e.g. what kind of security we expect (so that there's no ambiguity about whether we've succeeded or not)

One of the main goals of this course: learn about cryptographic objects AND some associated security properties!

Introduction 2021-02-03 14/29

#### Models are hard

- In crypto, it is common to have several security models for a single object
- For instance a block cipher may be analysed w.r.t. PRP, SPRP, XRKA-PRP, KCA... security or may further be assumed to be ideal!
- One needs to use a model appropriate for its actual use (symmetric encryption, building a tweakable block cipher, a compression function...)

Introduction 2021–02–03 15/29

### A quick model example

Indistiguishability in a chosen-plaintext setting (IND-CPA); fair model to decide if  $\mathbb{O}$  implements a good symmetric encryption scheme:

- $\blacksquare$  Submit messages to an  $\mathit{oracle} \ \mathbb O$  to be encrypted, & get the result
- 2 Choose,  $m_0$ ,  $m_1$  of equal length; send both to  $\mathbb{O}$
- $\square$  Receive  $\mathbb{O}(m_b)$  for a random  $b \in \{0,1\}$
- 4 Goal: determine the value of b (better than by guessing)
- ▶ 
   n has to be randomized

Introduction 2021–02–03 **16/29** 

### A code that's not IND-CPA



Figure: Calvin & Hobbes' code (Watterson)

Introduction 2021-02-03 17/29

### Randomness is key in crypto

#### Random numbers always needed

- ▶ To generate keys
- ▶ To generate initialization vectors (IVs) or nonces
- ► To generate random masks (to protect against some attacks)
- ► Etc.

Introduction 2021-02-03 18/29

### Random number generation is not easy

Lead to severe vulnerabilities, several times. For instance:

- ▶ Debian's OpenSSL key generation (2006–2008)
- WWW RSA private keys with shared factors (Lenstra et al., 2012)
- ► Smartcard RSA w/ biased private keys (Bernstein et al., 2013)
- ► Smartcard RSA w/ biased private keys (Nemec et al., 2017)

Introduction 2021-02-03 19/29

```
int getRandomNumber()
{
    return 4; // chosen by fair dice roll.
    // guaranteed to be random.
}
```

Figure: XKCD's PRNG (Munroe)

Introduction 2021–02–03 20/29

### How not to generate random numbers

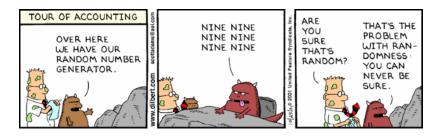


Figure: Dilbert's PRNG (Adams)

Very small Kolmogorov complexity!

Introduction 2021-02-03 20/29

### How to generate them, then?

A basic idea (e.g. /dev/urandom)

- ▶ Set up a "random" state (from e.g. physical sources)
- Refresh it continuously as randomness comes by
- Extract and filter when outputs are needed

Introduction 2021-02-03 21/29

# Are random numbers all you need?

A "perfect" encryption scheme, the one-time pad

- Let the message m be in  $\{0,1\}^n$ , n maybe large (say,  $2^{40}$ )
- **2** Let the key k be  $\leftarrow \{0,1\}^n$
- **3** The ciphertext  $c = m \oplus k$
- $\blacktriangleright$  Knowing c does not give information about m (see TD)

#### Problems:

- Integrity not guaranteed. So actually NOT perfect in presence of active adversaries (i.e. all the time)
- Needs very large keys
- ▶ Needs "perfect" randomness too!

Introduction 2021-02-03 22/29

# What do you need then? Symmetric primitives!

- Stream ciphers (computational variants of OTP), e.g. RC4 (broken), Trivium...
- Block ciphers (encrypt "blocks"), e.g. AES
- Message authentication codes (MACs, check authenticity), e.g. {A,B,C,D,E,F,G,H,I,K,L,M,N,O,P,Q,R,S,T,U,V,W,X,Z}MAC (For more on the topic, cf. https://www-ljk.imag.fr/ membres/Pierre.Karpman/JMAC.pdf)
- Hash functions (securely compress long messages to short digests), e.g. SHA-3

Also need, say, mode of operations (to get e.g. IND-CPA)

Introduction 2021–02–03 23/29

# Complementary primitives: public-key cryptography

Not all primitives need a single secret key. One can also have

- ► Trapdoor permutations (easy to encrypt, hard to decrypt w/o the trapdoor), e.g. RSA
- Public key exchange, e.g. Diffie-Hellman
- Signatures, e.g. DSA

Introduction 2021–02–03 24/29

### We also need assumptions!

Public-key schemes usually depend on "cryptographic assumptions" (= hardness of some problems), e.g.

- ► Factorization of large numbers (¬PQ)
- ▶ Computing discrete logarithms in  $\mathbb{F}_q^{\times}$ ,  $E(\mathbb{F}_q)$ , ...  $(\neg PQ)$
- Decoding a noisy codeword of a random error-correcting code (PQ)
- ► Finding a short vector in a lattice (PQ)
- Solving a quadratic system of equations (PQ)
- "Inverting" hash functions (PQ)
- ► Etc.

Note: Assumptions can be attacked!

Introduction 2021–02–03 25/29

# We need keys: secret, private, public...

### What are crypto keys like?

- Stream/Block cipher: a binary string
- ▶ Hash functions: ∅
- RSA: a prime number (secret), an integer (public)
- Diffie-Hellman: an integer (secret), a group element (public)
- Code-based: a (generating) matrix (of a linear code) (one secret, one public)
- Etc.

Introduction 2021–02–03 26/29

### Secrets large and small

What should the secret/public key size be (in bits)?

- ▶ Block ciphers?
- ► RSA?
- ▶ Diffie-Hellman (well-chosen  $\mathbb{F}_q^{\times}$ )?
- ▶ Diffie-Hellman (well-chosen  $E(\mathbb{F}_q)$ )?
- Code-based (McEliece, Binary Goppa codes)?

Introduction 2021–02–03 27/29

### Secrets large and small

What should the secret/public key size be (in bits)?

- ▶ Block ciphers: e.g. 128 bits
- RSA: e.g. 3072 bits
- ▶ Diffie-Hellman (well-chosen  $\mathbb{F}_q^{\times}$ ): e.g. 3072 bits
- ▶ Diffie-Hellman (well-chosen  $E(\mathbb{F}_q)$ ): e.g. 256 bits
- ► Code-based (McEliece, Binary Goppa codes)? e.g. 200 000 bytes

Introduction 2021–02–03 27/29

### Secrets large and small

What should the secret/public key size be (in bits)?

 $\Rightarrow$  Quite a complex matter! (Follow recommendations, e.g. from ANSSI!)

Introduction 2021–02–03 27/29

# What's 128 bits anyway?

Objective: run a function  $2^{128}$  times within 34 years ( $\approx 2^{30}$  seconds), assuming:

- ► Hardware at 2<sup>50</sup> iterations/s (that's pretty good)
- ► Trivially parallelizable (that's not always the case in practice)
- ▶ 1000 W per device, no overhead e.g. for cooling (that's pretty good)

 $\Rightarrow$ 

- $ightharpoonup 2^{128-50-30} \approx 2^{48}$  machines needed
- $ho pprox 280\,000\,000$  GW 'round the clock
  - $ho \approx 170\,000\,000$  EPR nuclear reactors

(Of course technology may improve, but this gives quite a safe margin. One must however be careful about the exact attack setting (more of that another day))

Introduction 2021–02–03 28/29

# That's all for today

#### Next week:

▶ Block ciphers: what, why, how?

Introduction 2021–02–03 29/29